## Calculus I TA Session

## October, 2023

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1. **(Implicity differentiation)** 108 A1 Midterm Problem 3 (b) Suppose function g has the following property

$$g(\sin 3x) = 2(g(x) + x)$$

for any real number x and g is differentiable at x = 0. Find g(0) and g'(0).

## 2. (Inverse differentiation) 110 (01-05) Midterm Problem 2

Let f(x) be a twice differentiable one-to-one function. Suppose that f(2) = 1, f'(2) = 3, f''(2) = e. Find the following value

$$\frac{d}{dx}f^{-1}(1)$$
 and  $\frac{d^2}{dx^2}f^{-1}(1)$ 

3. **(Extreme value)** 110 (01-05) Midterm Problem 2 Suppose that the equation

$$x^2\cos(xy) + e^{y^2} - 2x + y = 0$$

is satisfied by a differentiable function y(x) defined on an open interval I containing 1 such that y(1) = 0. Besides, we assume that y'' exists everywhere on I.

- (a) Compute y'(1).
- (b) Compute y''(1).
- (c) Does y(x) attain a local extremum at x = 1? if your answer is YES, tell the type of local extremum (local maximum or local minimum) and give your reason.

## 4. (MVT) 105A Midterm Problem 6

Suppose that f is a differentiable function. If f'(a) > 0 and f'(b) < 0, explain that there exists  $c \in (a, b)$  such that f'(c) = 0. (Note that f' may not be continuous.)